

# Polynomial

Example	Name	Terms
$\frac{7}{6x}$	monomial	1 term
$3t - 1$ $12xy^3 + 5x^4y$	binomial	2 terms
$2x^2 + 3x - 7$	trinomial	3 terms

Nonexample	Reason
$5m^0 - 8$	variable exponent
$n^{-3} + 9$	negative exponent

# Degree of a Polynomial

The largest exponent or the largest sum of exponents of a term within a polynomial

Polynomial	Degree of Each Term	Degree of Polynomial
$-7m^3n^5$	$-7m^3n^5 \rightarrow \text{degree } 8$	8
$2x + 3$	$2x \rightarrow \text{degree } 1$ $3 \rightarrow \text{degree } 0$	1
$6a^3 + 3a^2b^3 - 21$	$6a^3 \rightarrow \text{degree } 3$ $3a^2b^3 \rightarrow \text{degree } 5$ $-21 \rightarrow \text{degree } 0$	5

# Add Polynomials

## (Group Like Terms – Horizontal Method)

Example:

$$\begin{aligned} h(g) &= 2g^2 + 6g - 4; k(g) = g^2 - g \\ h(g) + k(g) &= (2g^2 + 6g - 4) + (g^2 - g) \\ &= \textcolor{red}{2g^2} + \textcolor{blue}{6g} - 4 + \textcolor{red}{g^2} - g \\ &\quad (\text{Group like terms and add}) \\ &= (\textcolor{red}{2g^2} + \textcolor{red}{g^2}) + (\textcolor{blue}{6g} - \textcolor{blue}{g}) - 4 \\ h(g) + k(g) &= 3g^2 + 5g - 4 \end{aligned}$$

# Add Polynomials

(Align Like Terms –  
Vertical Method)

Example:

$$h(g) = 2g^3 + 6g^2 - 4; k(g) = g^3 - g - 3$$

$$h(g) + k(g) = (2g^3 + 6g^2 - 4) + (g^3 - g - 3)$$

(Align like terms and add)

$$\begin{array}{r} 2g^3 + 6g^2 \quad - 4 \\ + \quad g^3 \quad \quad - g - 3 \\ \hline h(g) + k(g) = 3g^3 + 6g^2 - g - 7 \end{array}$$

# Subtract Polynomials

## (Group Like Terms - Horizontal Method)

Example:

$$f(x) = 4x^2 + 5; g(x) = -2x^2 + 4x - 7$$

$$f(x) - g(x) = (4x^2 + 5) - (-2x^2 + 4x - 7)$$

(Add the inverse)

$$= (4x^2 + 5) + (2x^2 - 4x + 7)$$

$$= \color{blue}{4x^2} + \color{red}{5} + \color{blue}{2x^2} - 4x + \color{red}{7}$$

(Group like terms and add.)

$$= (\color{blue}{4x^2} + \color{blue}{2x^2}) - 4x + (\color{red}{5} + \color{red}{7})$$

$$f(x) - g(x) = 6x^2 - 4x + 12$$

# Subtract Polynomials

## (Align Like Terms - Vertical Method)

Example:

$$f(x) = 4x^2 + 5; g(x) = -2x^2 + 4x - 7$$

$$f(x) - g(x) = (4x^2 + 5) - (-2x^2 + 4x - 7)$$

(Align like terms then add the inverse  
and add the like terms.)

$$\begin{array}{r} 4x^2 \quad \quad + 5 \quad \rightarrow \quad 4x^2 \quad \quad + 5 \\ -(-2x^2 + 4x - 7) \quad \rightarrow + \underline{2x^2 - 4x + 7} \\ \hline f(x) - g(x) = 6x^2 - 4x + 12 \end{array}$$

# Multiply Polynomials

Apply the distributive property.

$$(a + b)(d + e + f)$$

$$(a + b)(\textcolor{red}{d + e + f})$$

$$= \textcolor{blue}{a}(d + e + f) + \textcolor{blue}{b}(d + e + f)$$

$$= ad + ae + af + bd + be + bf$$

# Divide Polynomials

(Monomial Divisor)

Divide each term of the dividend by  
the monomial divisor

Example:

$$f(x) = 12x^3 - 36x^2 + 16x; g(x) = 4x$$

$$\begin{aligned}\frac{f(x)}{g(x)} &= (12x^3 - 36x^2 + 16x) \div \textcolor{red}{4x} \\ &= \frac{12x^3 - 36x^2 + 16x}{4x}\end{aligned}$$

$$= \frac{12x^3}{4x} - \frac{36x^2}{4x} + \frac{16x}{4x}$$

$$\frac{f(x)}{g(x)} = 3x^2 - 9x + 4$$

# Divide Polynomials

## (Binomial Divisor)

Factor and simplify

Example:

$$f(w) = 7w^2 + 3w - 4; g(w) = w + 1$$

$$\begin{aligned}\frac{f(w)}{g(w)} &= (7w^2 + 3w - 4) \div (w + 1) \\ &= \frac{7w^2 + 3w - 4}{w + 1}\end{aligned}$$

$$= \frac{(7w - 4)(w + 1)}{w + 1}$$

$$\frac{f(w)}{g(w)} = 7w - 4$$

# Prime Polynomial

Cannot be factored into a product of lesser degree polynomial factors

Example
$r$
$3t + 9$
$x^2 + 1$
$5y^2 - 4y + 3$

Nonexample	Factors
$x^2 - 4$	$(x + 2)(x - 2)$
$3x^2 - 3x - 6$	$3(x + 1)(x - 2)$
$x^3$	$x \cdot x^2$