System of Linear Equations (Number of Solutions)

Number of Solutions	Slopes and y-intercepts	Graph
One solution	Different slopes	<i>y</i>
No solution	Same slope and different - intercepts	y x
Infinitely many solutions	Same slope and same y-intercepts	<i>y</i>

System of Linear Equations

(Substitution)

$$\begin{cases} x + 4y = 17 \\ y = x - 2 \end{cases}$$

Substitute x - 2 for y in the first equation.

$$x + 4(x - 2) = 17$$
$$x = 5$$

Now substitute 5 for x in the second equation.

$$y = 5 - 2$$

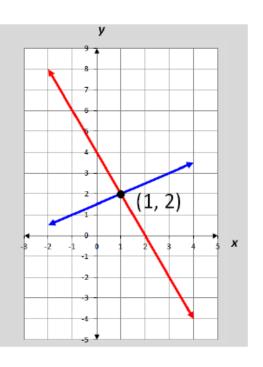
$$y = 3$$

The solution to the linear system is (5, 3), the ordered pair that satisfies both equations.

System of Linear **Equations** (Graphing) $\begin{cases} -x + 2y = 3 \\ 2x + y = 4 \end{cases}$

$$\begin{cases} -x + 2y = 3 \\ 2x + y = 4 \end{cases}$$

The solution, (1, 2), is the only ordered pair that satisfies both equations (the point of intersection).



System of Linear Equations (Elimination)

$$\begin{cases} -5x - 6y = 8 \\ 5x + 2y = 4 \end{cases}$$

Add or subtract the equations to eliminate one variable

$$-5x - 6y = 8$$

$$+ 5x + 2y = 4$$

$$-4y = 12$$

$$y = -3$$

Now substitute -3 for y in either original equation to find the value of x, the eliminated variable.

$$-5x - 6(-3) = 8$$

 $x = 2$

The solution to the linear system is (2,-3), the ordered pair that satisfies both equations.

System of Equations

(Linear - Quadratic)

$$\begin{cases} y = x + 1 \\ y = x^2 - 1 \end{cases}$$

The solutions, (-1,0) and (2,3), are the only ordered pairs that satisfy both equations (the points of intersection).

