

Horizontal and Vertical Asymptotes

1. A line $y = b$ is a horizontal asymptote of the graph $y = f(x)$ if either
$$\lim_{x \rightarrow \infty} f(x) = b \text{ or } \lim_{x \rightarrow -\infty} f(x) = b.$$
(Compare degrees of functions in fraction)
2. A line $x = a$ is a vertical asymptote of the graph $y = f(x)$ if either
$$\lim_{x \rightarrow a^+} f(x) = \pm\infty \text{ or } \lim_{x \rightarrow a^-} f(x) = \pm\infty$$
(Values that make the denominator 0 but not numerator)