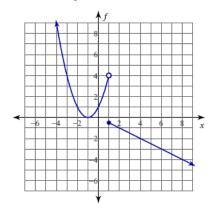
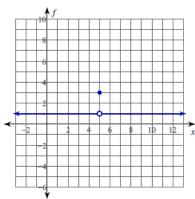
Find the intervals on which each function is continuous.

1) 
$$f(x) = \begin{cases} x^2 + 2x + 1, & x < 1 \\ -\frac{x}{2}, & x \ge 1 \end{cases}$$

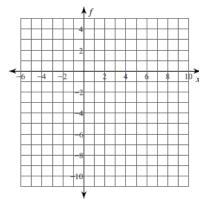


2) 
$$f(x) = \begin{cases} 1, & x \neq 5 \\ 3, & x = 5 \end{cases}$$

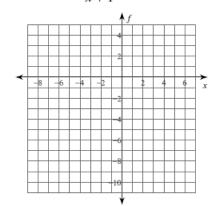


Find the intervals on which each function is continuous. You may use the provided graph to sketch the function.

3) 
$$f(x) = \begin{cases} 2x - 10, & x < 2 \\ 0, & x \ge 2 \end{cases}$$



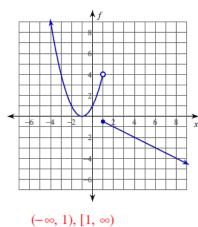
4) 
$$f(x) = \frac{x^2 - x - 2}{x + 1}$$



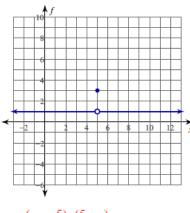
#### **Answers**

Find the intervals on which each function is continuous.

1) 
$$f(x) = \begin{cases} x^2 + 2x + 1, & x < 1 \\ -\frac{x}{2}, & x \ge 1 \end{cases}$$



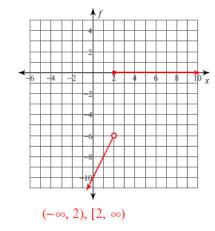
2) 
$$f(x) = \begin{cases} 1, & x \neq 5 \\ 3, & x = 5 \end{cases}$$



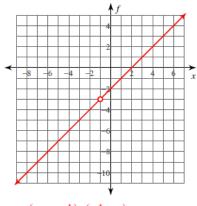
$$(-\infty, 5), (5, \infty)$$

 $Find the intervals on which each function is continuous. \ You may use the provided graph to sketch the function.$ 

3) 
$$f(x) = \begin{cases} 2x - 10, & x < 2 \\ 0, & x \ge 2 \end{cases}$$



4) 
$$f(x) = \frac{x^2 - x - 2}{x + 1}$$



$$(-\infty, -1), (-1, \infty)$$

Find the intervals on which each function is continuous.

$$5) f(x) = \frac{x^2}{2x+4}$$

6) 
$$f(x) = \begin{cases} -\frac{x}{2} - \frac{7}{2}, & x \le 0\\ -x^2 + 2x - 2, & x > 0 \end{cases}$$

7) 
$$f(x) = -\frac{x^2 - x - 12}{x + 3}$$

8) 
$$f(x) = \frac{x^2 - x - 6}{x + 2}$$

Determine if each function is continuous. If the function is not continuous, find the x-axis location of and classify each discontinuity.

9) 
$$f(x) = -\frac{x^2}{2x+4}$$

10) 
$$f(x) = \frac{x+1}{x^2-x-2}$$

11) 
$$f(x) = \frac{x+1}{x^2+x+1}$$

12) 
$$f(x) = -\frac{x^2}{x-1}$$

13) 
$$f(x) = \begin{cases} x^2 - 4x + 3, & x \neq 0 \\ 3, & x = 0 \end{cases}$$

14) 
$$f(x) = \begin{cases} -x^2, & x \neq 1 \\ 0, & x = 1 \end{cases}$$

Critical thinking questions:

- 15) Give an example of a function with discontinuities at x = 1, 2, and 3.
- 16) Of the six basic trigonometric functions, which are continuous over all real numbers? Which are not? What types of discontinuities are there?

#### Answers

Find the intervals on which each function is continuous.

5) 
$$f(x) = \frac{x^2}{2x+4}$$
  
 $(-\infty, -2), (-2, \infty)$ 

6) 
$$f(x) = \begin{cases} -\frac{x}{2} - \frac{7}{2}, & x \le 0\\ -x^2 + 2x - 2, & x > 0 \end{cases}$$

 $(-\infty, 0], (0, \infty)$ 

7) 
$$f(x) = -\frac{x^2 - x - 12}{x + 3}$$

$$(-\infty, -3), (-3, \infty)$$

8) 
$$f(x) = \frac{x^2 - x - 6}{x + 2}$$

$$(-\infty, -2), (-2, \infty)$$

Determine if each function is continuous. If the function is not continuous, find the x-axis location of and classify each discontinuity.

9) 
$$f(x) = -\frac{x^2}{2x+4}$$

Essential discontinuity at: 
$$x = -2$$

10) 
$$f(x) = \frac{x+1}{x^2-x-2}$$

Removable discontinuity at: x = -1Essential discontinuity at: x = 2

11) 
$$f(x) = \frac{x+1}{x^2+x+1}$$

12) 
$$f(x) = -\frac{x^2}{x-1}$$

Essential discontinuity at: x = 1

13) 
$$f(x) = \begin{cases} x^2 - 4x + 3, & x \neq 0 \\ 3, & x = 0 \end{cases}$$

14) 
$$f(x) = \begin{cases} -x^2, & x \neq 1 \\ 0, & x = 1 \end{cases}$$

Removable discontinuity at: x = 1

#### Critical thinking questions:

15) Give an example of a function with discontinuities at x = 1, 2, and 3.

Many answers. 
$$\frac{1}{(x-1)(x-2)(x-3)}$$

16) Of the six basic trigonometric functions, which are continuous over all real numbers? Which are not? What types of discontinuities are there?

Cont: sin, cos. Not cont: sec, csc, tan, cot. Essential.