

Antiderivatives (... Introduction to Integration) ... Set 2

Basic Integration Problems

I. Find the following integrals.

$$1. \int (5x^2 - 8x + 5)dx$$

$$2. \int (-6x^3 + 9x^2 + 4x - 3)dx$$

$$3. \int (x^{\frac{3}{2}} + 2x + 3)dx$$

$$4. \int \left(\frac{8}{x} - \frac{5}{x^2} + \frac{6}{x^3} \right) dx$$

$$5. \int (\sqrt{x} + \frac{1}{3\sqrt{x}})dx$$

$$6. \int (12x^{\frac{3}{4}} - 9x^{\frac{5}{3}})dx$$

$$7. \int \frac{x^2 + 4}{x^2} dx$$

$$8. \int \frac{1}{x\sqrt{x}} dx$$

$$9. \int (1 + 3t)t^2 dt$$

$$10. \int (2t^2 - 1)^2 dt$$

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Answers

I. Find the following integrals.

1. $\int (5x^2 - 8x + 5)dx = \boxed{\frac{5x^3}{3} - 4x^2 + 5x + C}$

2. $\int (-6x^3 + 9x^2 + 4x - 3)dx = \boxed{\frac{-3x^4}{2} + 3x^3 + 2x^2 - 3x + C}$

3. $\int (x^{\frac{3}{2}} + 2x + 3)dx = \boxed{\frac{2x^{\frac{5}{2}}}{5} + x^2 + 3x + C}$

4.
$$\begin{aligned} \int \left(\frac{8}{x} - \frac{5}{x^2} + \frac{6}{x^3} \right) dx &= \int \left(\frac{8}{x} - 5x^{-2} + 6x^{-3} \right) dx \\ &= 8\ln(x) - \frac{5x^{-1}}{-1} + \frac{6x^{-2}}{-2} = \boxed{8\ln(x) + \frac{5}{x} - \frac{3}{x^2} + C} \end{aligned}$$

5.
$$\begin{aligned} \int (\sqrt{x} + \frac{1}{3\sqrt{x}})dx &= \int \left(x^{\frac{1}{2}} + \frac{1}{3}x^{-\frac{1}{2}} \right) dx \\ &= \frac{x^{\frac{3}{2}}}{\frac{3}{2}} + \frac{1}{3} \cdot \frac{x^{\frac{1}{2}}}{\frac{1}{2}} = \boxed{\frac{2}{3}x^{\frac{3}{2}} + \frac{2}{3}x^{\frac{1}{2}} + C} \end{aligned}$$

6.
$$\int (12x^{\frac{3}{4}} - 9x^{\frac{5}{4}})dx = \boxed{\frac{48x^{\frac{7}{4}}}{7} - \frac{27x^{\frac{9}{4}}}{8} + c}$$

7.
$$\int \frac{x^2 + 4}{x^2} dx = \int 1 + 4x^{-2} dx = \boxed{x - \frac{4}{x} + C}$$

8.
$$\int \frac{1}{x\sqrt{x}} dx = \int x^{-\frac{3}{2}} dx = \boxed{-\frac{2}{\sqrt{x}} + C}$$

9.
$$\int (1+3t)t^2 dt = \int t^2 + 3t^3 dt = \boxed{\frac{t^3}{3} + \frac{3t^4}{4} + C}$$

10.
$$\int (2t^2 - 1)^2 dt = \int 4t^4 - 4t^2 + 1 dt = \boxed{\frac{4t^5}{5} - \frac{4t^3}{3} + t + C}$$

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$$11. \int y^2 \sqrt[3]{y} dy$$

$$12. \int d\theta$$

$$13. \int 7 \sin(x) dx$$

$$14. \int 5 \cos(\theta) d\theta$$

$$15. \int 9 \sin(3x) dx$$

$$16. \int 12 \cos(4\theta) d\theta$$

$$17. \int 7 \cos(5x) dx$$

$$18. \int 4 \sin\left(\frac{x}{3}\right) dx$$

$$19. \int 4e^{-7x} dx$$

$$20. \int 9e^{\frac{x}{4}} dx$$

$$21. \int -5 \cos \pi x dx$$

$$22. \int -13e^{6t} dt$$

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Answers

$$11. \int y^2 \sqrt[3]{y} dy = \int y^{\frac{7}{3}} dy = \boxed{\frac{3y^{\frac{10}{3}}}{10} + C}$$

$$12. \int d\theta = \boxed{\theta + C}$$

$$13. \int 7 \sin(x) dx = \boxed{-7 \cos(x) + C}$$

$$14. \int 5 \cos(\theta) d\theta = \boxed{5 \sin(\theta) + C}$$

$$15. \int 9 \sin(3x) dx = \boxed{-3 \cos(3x) + C}$$

$$16. \int 12 \cos(4\theta) d\theta = \boxed{3 \sin 4\theta + C}$$

$$17. \int 7 \cos(5x) dx = \boxed{\frac{7 \sin(5x)}{5} + C}$$

$$18. \int 4 \sin\left(\frac{x}{3}\right) dx = \boxed{-12 \cos\left(\frac{x}{3}\right) + C}$$

$$19. \int 4e^{-7x} dx = \boxed{-\frac{4e^{-7x}}{7} + C}$$

$$20. \int 9e^{\frac{x}{4}} dx = \boxed{36e^{\frac{x}{4}} + C}$$

$$21. \int -5 \cos \pi x dx = \boxed{-\frac{5 \sin(\pi x)}{\pi} + C}$$

$$22. \int -13e^{6t} dt = \boxed{-\frac{13e^{6t}}{6} + C}$$

Antiderivatives (... Introduction to Integration) ... Set 2

II. Evaluate the following definite integrals.

$$1. \int_1^4 (5x^2 - 8x + 5)dx$$

$$2. \int_1^9 (x^{\frac{3}{2}} + 2x + 3)dx$$

$$3. \int_4^9 (\sqrt{x} + \frac{1}{3\sqrt{x}})dx$$

$$4. \int_1^4 \frac{5}{x^3} dx$$

$$5. \int_{-1}^2 (1+3t)t^2 dt$$

$$6. \int_{-2}^1 (2t^2 - 1)^2 dt$$

Antiderivatives (... Introduction to Integration) ... Set 2

Answers

II. Evaluate the following definite integrals.

$$1. \int_1^4 (5x^2 - 8x + 5)dx = \left(\frac{5x^3}{3} - 4x^2 + 5x \right)_1^4 = \frac{188}{3} - \frac{8}{3} = \boxed{60}$$

$$2. \int_1^9 (x^{\frac{5}{2}} + 2x + 3)dx = \left(\frac{2x^{\frac{5}{2}}}{5} + x^2 + 3x \right)_1^9 = \frac{1026}{5} - \frac{22}{5} = \boxed{\frac{1001}{5} = 200.2}$$

$$3. \int_4^9 (\sqrt{x} + \frac{1}{3\sqrt{x}})dx = \left(\frac{2}{3}x^{\frac{3}{2}} + \frac{2}{3}x^{\frac{1}{2}} \right)_4^9 = 20 - \frac{20}{3} = \boxed{\frac{40}{3} = 13.333}$$

$$4. \int_1^4 \frac{5}{x^3} dx = -\frac{5}{2x^2} \Big|_1^4 = -\frac{5}{32} + \frac{5}{2} = \boxed{\frac{75}{32} = 2.344}$$

$$5. \int_{-1}^2 (1+3t)t^2 dt = \left(\frac{t^3}{3} + \frac{3t^4}{4} \right)_{-1}^2 = \frac{44}{3} - \frac{5}{12} = \boxed{\frac{57}{4} = 14.25}$$

$$6. \int_{-2}^1 (2t^2 - 1)^2 dt = \left(\frac{4t^5}{5} - \frac{4t^3}{3} + t \right)_{-2}^1 = \frac{7}{15} + \frac{254}{15} = \boxed{\frac{87}{5} = 17.4}$$