### Base e Exponential Functions ... Set 1

Math 3

# Natural Logarithms & Base e

SWBAT solve logarithmic equations involving natural logs and base e.

Evaluate Natural Base Expressions:

\*simply type "2nd ex (insert number) enter" in your calculator\*

- a)  $e^{0}$
- b)  $e^{-8}$
- c)  $e^2$
- d)  $e^{-1.3}$

Example 1: Simplify the expression

- $\frac{\ln e^4}{8}$
- b)  $\ln e^{83}$

Natural base exponential function:  $y = e^x$ 

#### Natural Logarithm:

logarithm with base e

Natural logarithm function:  $y = \ln x$ 

Example 3: Write each expression as a single natural logarithm.
Use the properties of logs to condense!

- a)  $3 \ln 5$
- b)  $\ln 24 \ln 6$
- c)  $\frac{1}{3}(\ln x + \ln y) 4\ln z$
- d)  $2 \ln 8 3 \ln 4$

Evaluate Natural Base Expressions:

\*simply type "In (insert number) enter" in your calculator\*

- a) In 3
- b)  $\ln \frac{1}{4}$
- c) ln 4
- d) In 0.05

Example 2: Simplify the expression

- a)  $10 \ln e$
- b) ln1

Example 4: Solve Base *e* Equations

After isolating the e, use In on each side to cancel out the e

a) 
$$e^{\frac{x}{4}} + 3 = 9$$

b) 
$$5e^{-x} - 7 = 2$$

c) 
$$3e^{-2x} + 4 = 10$$

d) 
$$e^{3x+1} = e^{13}$$

**Example 5: Solve Natural Log Equations** 

After isolating the In, use e on each side to cancel out the In

a) 
$$\ln 5 - \ln x = 4$$

b) 
$$ln(2m+3) = 8$$

c) 
$$\ln \frac{x-3}{4} = 8$$

$$d) \quad 3\ln 3x^2 = 1$$

## Base e Exponential Functions ... Set 1

Applications of Natural Logs and Base e  $\underline{\ \ }^{***} \text{To calculate continuously compounded interest, we use the formula:}$ 

P=

**†** =

Example 6: How much money will be in a bank account after 1.5 years if you invested \$400 at 7.6% compounded continuously?

Practice: Complete the following problems for class work. Show all work.

1. Solve 
$$\ln(14x - 3) = \ln(7x + 11)$$

2. Solve 
$$2e^x - 5 = 1$$

3. 
$$ln(x-1) = -2$$

4. 
$$\ln(2x-3) = 2.5$$

6. 
$$e^{3x} \cdot e^x = 15$$

Mixed Review: Remember, all logarithms share the same rules. Always condense first before solving!

7. 
$$4^{3x} = 12$$

8. 
$$log_6 x + log_6 9 = log_6 54$$

9. 
$$\log_2 x = -3$$

11. 
$$\log_2 x - \log_2 5 = 3$$

12. 
$$\ln 4x + \ln 5 = \ln 20$$

13. Mazie invested \$4500 in an account earning 4.3% interest compounded continuously. After how many years will she have \$7400 in her account?