# **Practice Test**

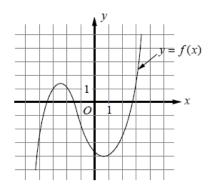
## Polynomials Functions

1

If the graph of  $f(x) = 2x^3 + bx^2 + 4x - 4$  intersects the x-axis at  $(\frac{1}{2}, 0)$ , and (-2, k) lies on the graph of f, what is the value of k?

- A) -4
- B) -2
- C) 0
- D) 2

2



The function y = f(x) is graphed on the xy-plane above. If k is a constant such that the equation f(x) = k has one real solution, which of the following could be the value of k?

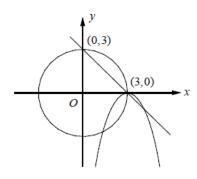
- A) -3
- B) -1
- C) 1
- D) 3

3

What is the value of a if x + 2 is a factor of  $f(x) = -(x^3 + 3x^2) - 4(x - a)$ ?

- A) -2
- B) -1
- C) 0
- D) 1

4



$$x^{2} + y^{2} = 9$$
$$y = -(x-3)^{2}$$

A system of three equations and their graphs on the *xy*-plane are shown above. How many solutions does the system have?

- A) 1
- B) 2
- C) 3
- D) 4

#### 5

Which of the following complex numbers is equivalent to  $\frac{(1-i)^2}{1+i}$ ?

- A)  $-\frac{i}{2} \frac{1}{2}$
- B)  $-\frac{i}{2} + \frac{1}{2}$
- C) -i-1
- D) -i+1

#### 6

Which of the following is equal to  $a \sqrt[3]{a}$ ?

- A)  $a^{\frac{2}{3}}$
- B)  $a^{\frac{4}{3}}$
- C)  $a^{\frac{5}{3}}$
- D)  $a^{\frac{7}{3}}$

#### 7

$$p(x) = -2x^{3} + 4x^{2} - 10x$$
$$q(x) = x^{2} - 2x + 5$$

The polynomials p(x) and q(x) are defined above. Which of the following polynomials is divisible by x-1?

- A)  $f(x) = p(x) \frac{1}{2}q(x)$
- B)  $g(x) = -\frac{1}{2}p(x) q(x)$
- C)  $h(x) = -p(x) + \frac{1}{2}q(x)$
- D)  $k(x) = \frac{1}{2}p(x) + q(x)$

#### 8

$$\sqrt{2x+6} = x+3$$

What is the solution set of the equation above?

- A)  $\{-3\}$
- B) {-1}
- C)  $\{-3, 2\}$
- D)  $\{-3, -1\}$

#### 9

What is the remainder when polynomial

$$p(x) = 24x^3 - 36x^2 + 14$$
 is divided by  $x - \frac{1}{2}$ ?

- A) 4
- B) 6
- C) 8
- D) 10

#### 10

The function f is defined by a polynomial. If x+2, x+1, and x-1 are factors of f, which of the following table could define f?

	Δ	ı	١	
•	•		,	
				ı

1		
	х	f(x)
	-2	4
	-1	0
	1	0
	2	0

B)

•	
x	f(x)
-2	0
-1	4
1	0
2	0

C)

,		
	х	f(x)
	-2	0
	-1	0
	1	4
	2	0

D)

"	)		
	x	f(x)	
	-2	0	
	-1	0	
	1	0	
ſ	2	4	

# Answers Polynomials Functions

#### 1. C

$$f(x) = 2x^3 + bx^2 + 4x - 4$$

$$f(\frac{1}{2}) = 0$$
 because the graph of f intersects the

x-axis at 
$$(\frac{1}{2}, 0)$$
.

$$f(\frac{1}{2}) = 2(\frac{1}{2})^3 + b(\frac{1}{2})^2 + 4(\frac{1}{2}) - 4 = 0$$

Solving the equation for b gives b = 7.

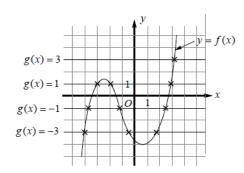
Thus 
$$f(x) = 2x^3 + 7x^2 + 4x - 4$$
.

Also k = f(-2), because (-2, k) lies on the graph of f.

$$k = f(-2) = 2(-2)^3 + 7(-2)^2 + 4(-2) - 4$$

Solving the equation for k gives k = 0.

#### 2. D



g(x) = -3 has 3 points of intersection with

y = f(x), so there are 3 real solutions.

g(x) = -1 has 3 points of intersection with

y = f(x), so there are 3 real solutions.

g(x) = 1 has 3 points of intersection with

y = f(x), so there are 3 real solutions.

g(x) = 3 has 1 point of intersection with

y = f(x), so there is 1 real solution.

Choice D is correct

#### 3. B

If 
$$x + 2$$
 is a factor of

$$f(x) = -(x^3 + 3x^2) - 4(x - a)$$
, then  $f(-2) = 0$ .

$$f(-2) = -((-2)^3 + 3(-2)^2) - 4(-2 - a) = 0$$

$$-(-8+12)+8+4a=0$$

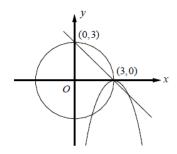
$$4+4a=0$$

$$a = -1$$

### Answers

## Polynomials Functions

#### 4. A



The solutions to the system of equations are the points where the circle, parabola, and line all intersect. That point is (3,0) and is therefore the only solution to the system.

#### 5. C

$$\frac{(1-i)^2}{1+i}$$

$$=\frac{1-2i+i^2}{1+i}$$
FOIL the numerator.
$$=\frac{1-2i-1}{1+i}$$

$$=\frac{-2i}{1+i}$$
Simplify.
$$=\frac{-2i}{1+i}\cdot\frac{1-i}{1-i}$$
Rationalize the denominator.
$$=\frac{-2i+2i^2}{1-i^2}$$
FOIL
$$=\frac{-2i-2}{2}$$

$$=-i-1$$

#### 6. B

$$a\sqrt[3]{a} = a \cdot a^{\frac{1}{3}} = a^{1+\frac{1}{3}} = a^{\frac{4}{3}}$$

#### 7. B

$$p(x) = -2x^{3} + 4x^{2} - 10x$$
$$q(x) = x^{2} - 2x + 5$$

In p(x), factoring out the GCF, -2x, yields  $p(x) = -2x(x^2 - 2x + 5) = -2x \cdot q(x).$ 

Let's check each answer choice.

A) 
$$f(x) = p(x) - \frac{1}{2}q(x)$$
  
=  $-2x \cdot q(x) - \frac{1}{2}q(x) = (-2x - \frac{1}{2})q(x)$ 

q(x) is not a factor of x-1 and  $(-2x-\frac{1}{2})$  is not a factor of x-1. f(x) is not divisible by x-1.

B) 
$$g(x) = -\frac{1}{2}p(x) - q(x)$$
  
=  $-\frac{1}{2}[-2x \cdot q(x)] - q(x) = (x-1)q(x)$ 

Since g(x) is x-1 times q(x), g(x) is divisible by x-1.

Choices C and D are incorrect because x-1 is not a factor of the polynomials h(x) and k(x).

#### 8. D

$$\sqrt{2x+6} = x+3$$

$$(\sqrt{2x+6})^2 = (x+3)^2$$
Square each side.
$$2x+6 = x^2+6x+9$$
Simplify.
$$x^2+4x+3=0$$
Make one side 0.
$$(x+1)(x+3)=0$$
Factor.
$$x+1=0 \text{ or } x+3=0$$
Zero Product Property
$$x=-1 \text{ or } x=-3$$

Check each x-value in the original equation.

$$\sqrt{2(-1)+6} = -1+3$$
  $x = -1$   
 $\sqrt{4} = 2$  Simplify.  
 $2 = 2$  True  
 $\sqrt{2(-3)+6} = -3+3$   $x = -3$   
 $0 = 0$  True

Thus, -1 and -3 are both solutions to the equation.

#### 9. C

Use the remainder theorem.

$$p(\frac{1}{2}) = 24(\frac{1}{2})^3 - 36(\frac{1}{2})^2 + 14 = 8$$

Therefore, the remainder of polynomial

$$p(x) = 24x^3 - 36x^2 + 14$$
 divided by  $x - \frac{1}{2}$  is 8.

#### 10. D

If (x-a) is a factor of f(x), then f(a) must equal to 0. Thus, if x+2, x+1 and x-1 are factors of f, we have f(-2) = f(-1) = f(1) = 0.

Choice D is correct.